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Sliding Mode Stabilization of Quad Tilt-wing UAV Considering Nonlinear Model of the Vehicle and Uncertainties

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ABSTRACT

Keywords: Quadrotor UAV, VTOL, Morphing wing, MIMO systems, Robust control.

In this paper, a multi-input/multi-output sliding controller is proposed and analyzed for a quad tilt-wing unmanned aerial vehicle (QTW-UAV). The vehicle is equipped to do take-off and landing in vertical flight mode and is capable of flight over long distances in horizontal flight mode. The full dynamic model of the vehicle is originated from the Newton-Euler formulation. For developing the controller, a set of integral type sliding surfaces is selected and it is necessary to mention that in this approach, there is no linearization during controller design. Simulation has been conducted for a nonlinear, multivariable model that includes uncertain parameters and in the presence of pitch angle measurement noise and pitch moment disturbance. For verification, the proposed controller is compared with linear based controller design simulation. Results exhibit that the proposed controller is robust in the face of uncertainties, noise, and disturbance and meets performance demands with control inputs of low amplitude.

Nomenclature

m Mass Ι Identity matrix Diagonal inertia matrix I_h V_i Linear velocity in the inertial frame Ω_h Angular velocity in the body frame $F_{(.)}$ Force $M_{(.)}$ Moment $R_{(.)}$ Rotational matrix Gravity acceleration g Effective angle of attack α_i Tilt angle Θ Rotor rotational speed ω_i Velocity $V_{(.)}$ C_D Drag coefficient Lift coefficient C_L

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ρ	Air density
A	Area of wing
J_{prop}	Rotor rotational inertia
T_i	Rotor reaction torque
М	Inertia matrix
С	Coriolis-centripetal matrix
u_i	Control commands
p,q,r	Angular velocity about axis
ϕ, θ, ψ	Euler angles
X, Y, Z	Positions
S	Sliding surface
е	Error
Φ	Sliding boundary layer
Δ	Variance

Introduction

Due to the development of fly robots in the last decade, their participation in urban and non-urban services has increased, for example, remote sensing services in precision agriculture, forest health monitoring, air traffic control, mapping [1], borders security [2], traffic surveillance [3], power line monitoring [4], parcel delivery [5], aerial attack, etc, Furthermore, indoor missions like imaging, search and rescue among the tasks that are assigned to them.

To accomplish these missions, the drones are used. Unmanned Aerial Vehicles (UAV) can be categorized in terms of wing structure into two main classes: fixed-wing UAVs, and rotary-wing UAVs, and each type has its own advantages and drawbacks [6]. Fixed-wing UAVs have high cruising speed and altitude. They can fly as the long-range endurance and are able to carry heavy payload because of their large cabin capacity. However, requiring some equipment and runway for take-off and landing are restrictions of fixedwing UAVs. Rotary-wing UAVs, on the other hand, can vertically take-off and land (VTOL) without any required substructure. Also, they do not require any airflow for maneuvering. But they have lower speeds and range of flight.

Morphing technology can now combine these advantages by a hybrid design of the wing. In the tree diagram of the morphing technology illustrated in Figure 1, there are several techniques for the hybrid wing design of an aircraft such as survey of a wing-sweep morphing aircraft [7], Albatrosses biologically inspired morphing in shape as sweep and size as span extension [8], bionic bird wing-foldable UAV [9], Z-shaped morphing-wing [10], etc., but among these techniques, we deal with the rotation of the whole wing in incidence. This configuration is in the subdirectory of the rotating wing named tilt-wing. This hybrid design combines the vertical flight capabilities of rotary-wing UAVs with the highspeed cruise flight of fixed-wing UAVs. Given all the benefits of this design, there are disadvantages such as the high complexity of the vehicle's dynamics and the cost and the weight of the hinge and the rotation equipment.



Figure 1: Categorization of morphing aircraft technology [11].

There are several designs in the tilt-wing category such as new-style distributed propulsion tilt-wing UAV [12], albatross-inspired tilt-wing UAV [8], [13], tilt-wing rotorcraft [14], single tilt-wing [15], tilt-wing aircraft [16], A^3 Vahana VTOL tilt-wing [17], etc. In this paper, among different configuration designs of the tilt-wing, the quad tiltwing (QTW) is selected as the baseline (see Figure 2). In the selected configuration, there are four rotors on the leading edges of four wings with ability to tilt about their transverse axes. Despite the complexity and difficult control of QTW, there has been an extensive research on this field in recent years.

Some of these research focused on the aerodynamic characteristics and design [18], [19], other studies such as [20], configured Kalman filter-based linear quadratic integral (LQI) control method, and [21] designed an LQR and SMC with

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recursive implementation, which for LQR the dynamic equations of the vehicle are linearized around nominal operating points in hovering condition. In [22], [23] robust hovering and position PID type controllers on linear dynamical model under modeled aerodynamic disturbances are developed. Moreover, the studies [24], [25], focused on design and developed a novel quad tiltwing and analyzed it with hierarchical control system design. Also, [26] applied a PID controller on Sabanci University Unmanned Aerial Vehicle (SUAVI). Several studies work on Stability Augmentation System (SAS) and gain-scheduled flight controller of the QTW, e.g. [27]-[29]. Hierarchical adaptive control approach is considered in [30], [31]. The dynamic inversion method, which is a linearization method without an approximation algorithm is clarified in [32]. The research series [33]–[35], studied the stability and control augmentation system (SAS and CAS). Linear Quadratic Gaussian (LOG) control design on a nonlinear dynamical model in the presence of aerodynamic disturbances is developed in [36]. Further, from former authors a Model Predictive Control (MPC) design is expressed in another study [37] and an advanced Computer Aided Design (CAD) methodology for Processor-In-the-Loop (PIL) co-simulation and rapid control prototyping of a QTW is stated in [38]. In studies [40] a fuzzy Gain-Scheduled [39] and Proportional-Integral-Derivative (GS-PID) and a Linear Quadratic Gaussian (LQG) controller are configured, respectively. And recent studies, used Dynamic Inversion (DI), this is one example of the linearization method suggested for the UAVs proposed in [41], and an H_{∞} controller applied to dynamical model linearized QTW by Dynamic Inversion (DI) method is suggested in study [42]. The above-mentioned studies showed promising successful results. However, some of them use linearization or approximation in vehicle model or control development process and do not analyze the simulation in the presence of uncertainties.

In this study, a multi-input/multi-output SMC is presented without any linearization in design process nor any approximation in the modeling of QTW. This control approach is acceptable in amplitude of control signals in the presence of modeling imprecision. To show the necessity of using a controller based on nonlinear model, a SMC controller with respect to linear model is conducted on the nonlinear model and its results in the presence of uncertainties, sensor noise, and aerodynamic perturbations are compared with the results of the main control design.

This paper is organized as follows: In Section 2, the model of an aerial vehicle considering nonlinearities is provided. The flight controller of aerial vehicle is designed in Section 3. Simulation results are presented in Section 4, and finally, a conclusion and some future work are drawn in Section 5.

System Model

The aerial vehicle's nonlinear 6 DOF equations of motion including 3 DOF equations in transitional motion and 3 DOF equations in rotational motion are derived using Newton-Euler formulation. For a general unmanned aerial vehicle system, the equations of motion assuming that the vehicle is a rigid body can be written as

$$\begin{bmatrix} mI & 0\\ 0 & I_b \end{bmatrix} \begin{bmatrix} \dot{V}_i\\ \dot{\Omega}_b \end{bmatrix} + \begin{bmatrix} 0\\ \Omega_b \times (I_b \Omega_b) \end{bmatrix} = \begin{bmatrix} F_t\\ M_t \end{bmatrix}$$
(1)

Where the subscripts used as *b* and *i* represent the quantities in body and inertial frames, respectively. *m*, *I*, and 0 denote the mass, identity, and zero 3×3 matrices, respectively. Also I_b implies the diagonal inertia matrix of the UAV in the body frame. The linear velocity in the inertial frame and the angular velocity in the body frame of the UAV are represented by V_i and Ω_b , respectively. The left hand side of (1) is standard for many aerial vehicles; however, the net force and the moment terms, F_t and M_t , are case dependent (Figure 2).



Figure 2: The forces and moments that act on the vehicle [25].

It should be pointed out that for tilt-wing quadrotors, the net external force F_t is composed of the gravity force on the vehicle F_{grav} , motor thrusts F_{thru} , aerodynamic forces applied on the wings and the fuselage F_{aero} and external disturbances like winds and gusts F_{dist} . These sources of force are functions of the effective wing angle of attacks (Figure 3). It must be stated that the forces are distributed in the body coordinate

frame and it is desired to be transformed to inertial frame distribution via the rotational matrix R_{b2i} as follows:

$$F_t = R_{b2i}(F_{grav} + F_{thru} + F_{aero} + F_{dist})$$
(2)

Where,



Figure 3: Effective angle of attack α_i ; i = 1, 2, 3, 4.

$$F_{grav} = \begin{bmatrix} -S_{\theta} \\ S_{\phi} C_{\theta} \\ C_{\phi} C_{\theta} \end{bmatrix} mg \tag{4}$$

$$F_{thru} = \begin{bmatrix} c_{\Theta_1} & c_{\Theta_2} & c_{\Theta_3} & c_{\Theta_4} \\ 0 & 0 & 0 & 0 \\ -s_{\Theta_1} & -s_{\Theta_2} & -s_{\Theta_3} & -s_{\Theta_4} \end{bmatrix} \begin{bmatrix} k\omega_1^2 \\ k\omega_2^2 \\ k\omega_3^2 \\ k\omega_4^2 \end{bmatrix}$$
(5)

And

$$F_{aero} = \begin{bmatrix} F_{aero_x} \\ F_{aero_y} \\ F_{aero_z} \end{bmatrix} = \begin{bmatrix} F_{D_1} + F_{D_2} + F_{D_3} + F_{D_4} \\ 0 \\ F_{L_1} + F_{L_2} + F_{L_3} + F_{L_4} \end{bmatrix}$$
(6)

In these equations, c_{O} and s_{O} imply cos () and sin (), respectively. Θ_i (i = 1, 2, 3, 4) denotes the wing tilt angle with regard to the x body axis. It should be emphasized that the motor thrusts are modeled as $k\omega_i^2$, where the rotor rotational speed notation is as ω_i .

It is important to note that the lift and drag forces are expressed in the wind frame and have to be transformed via rotational matrix with respect to effective angle of attack as R_{w2b} . Where w expresses the quantities in the wind frame.

$$R_{b2w} = \begin{bmatrix} c_{\alpha_i} & s_{\alpha_i} & 0\\ -s_{\alpha_i} & c_{\alpha_i} & 0\\ 0 & 0 & 1 \end{bmatrix}$$
(7)

That

$$\alpha_{i} = \Theta_{i} - \left(-\arctan\left(V_{\alpha_{z}}, V_{\alpha_{x}}\right)\right)$$
(8)

$$R_{w2b} = (R_{b2w})^{-1} (9)$$

so with respect to (7) and (9), forces can be written as:

$$\begin{bmatrix} F_{D_i} \\ 0 \\ F_{L_i} \end{bmatrix} = R_{w2b} \begin{bmatrix} -\frac{1}{2}C_D\rho AV_{\alpha}^2 \\ 0 \\ -\frac{1}{2}C_L\rho AV_{\alpha}^2 \end{bmatrix}$$
(10)

That

$$V_{\alpha} = \sqrt{V_{\alpha_x}^2 + V_{\alpha_z}^2} \tag{11}$$

in the equation (10), C_D , and C_L are aerodynamics coefficient of drag and lift, respectively. Also ρ is the air density, A is the platform area of wing and V_{α} is the airflow velocity.

The total moment M_t consists of the moments created by the propellers gyroscopic effects M_{gyro} , the moments made by the rotors M_{thru} , aerodynamic forces M_{aero} and finally torques due to external disturbances M_{dist} .

$$M_t = M_{gyro} + M_{thru} + M_{aero} + M_{dist}$$
(12)
Where

Where,

$$M_{gyro} = \sum_{i=1}^{4} \left(J_{prop} \left[\eta_i \Omega_b \times \begin{bmatrix} c_{\Theta_i} \\ 0 \\ -s_{\Theta_i} \end{bmatrix} \omega_i \right] \right)$$
(13)

$$M_{thru} = l_{s} \begin{bmatrix} s_{\Theta_{1}} - \frac{\lambda_{1}}{l_{s}}c_{\Theta_{1}} & -s_{\Theta_{2}} - \frac{\lambda_{2}}{l_{s}}c_{\Theta_{2}} & s_{\Theta_{3}} - \frac{\lambda_{3}}{l_{s}}c_{\Theta_{3}} & -s_{\Theta_{4}} - \frac{\lambda_{4}}{l_{s}}c_{\Theta_{4}} \\ \frac{l_{t}}{l_{s}}s_{\Theta_{1}} & \frac{l_{t}}{l_{s}}s_{\Theta_{2}} & -\frac{l_{t}}{l_{s}}s_{\Theta_{3}} & -\frac{l_{t}}{l_{s}}s_{\Theta_{4}} \\ c_{\Theta_{1}} + \frac{\lambda_{1}}{l_{s}}s_{\Theta_{1}} & -c_{\Theta_{2}} + \frac{\lambda_{2}}{l_{s}}s_{\Theta_{2}} & c_{\Theta_{3}} + \frac{\lambda_{3}}{l_{s}}s_{\Theta_{3}} & -c_{\Theta_{4}} + \frac{\lambda_{4}}{l_{s}}s_{\Theta_{4}} \end{bmatrix} \\ \times \begin{bmatrix} k\omega_{2}^{2} \\ k\omega_{2}^{2} \\ k\omega_{2}^{2} \\ k\omega_{2}^{2} \end{bmatrix}$$

And

$$M_{aero} = \begin{bmatrix} M_{aero_x} \\ M_{aero_y} \\ M_{aero_z} \end{bmatrix}$$

$$= \begin{bmatrix} l_s(F_{L_1} - F_{L_2} + F_{L_3} - F_{L_4}) \\ l_l(F_{L_1} + F_{L_2} - F_{L_3} - F_{L_4}) \\ l_s(-F_{D_1} + F_{D_2} - F_{D_3} + F_{D_4}) \end{bmatrix}$$
(15)

In these expressions, J_{prop} is the rotational inertia of the rotors about their rotational axes, η_i is the sign of rotors rotation that is equal to 1, -1, -1, 1for rotor numbers 1,2,3, and 4, respectively (see Figure 2). l_s and l_l indicate the span-wise and longitudinal distances between the rotor axes and mass center of vehicle, respectively. Furthermore, the rotor reaction torques are considered as $T_i = \lambda_i k \omega_i^2$, where λ_i is the ratio of torque to force. In the way that for clockwise rotating propellers, $\lambda_{2,3} = -\lambda$, whilst for counterclockwise propellers $\lambda_{1,4} = \lambda$.

Using vector-matrix notation, (1) is rewritable as follows:

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$$M\dot{\zeta} + C(\zeta)\zeta = G + O(\zeta)\omega + E(\xi)\omega^{2} + W(\zeta) + D(\zeta,\xi)$$
(16)

Where $\zeta = [\dot{X} \ \dot{Y} \ \dot{Z} \ p \ q \ r]^T$ is the generalized velocity vector and $\xi = [X \ Y \ Z \ \phi \ \theta \ \psi]^T$ is the position and the orientation of center of mass with respect to the inertial frame. *M* and *C*(ζ) are the inertia matrix and Coriolis-centripetal matrix, respectively.

$$M = \begin{bmatrix} mI_{3\times3} & 0_{3\times3} \\ 0_{3\times3} & diag(I_{xx}, I_{yy}, I_{zz}) \end{bmatrix}$$
(17)
$$C(\zeta)$$
(18)

, and in right-hand side of (16), terms G, $O(\zeta)\omega$, $E(\xi)\omega^2$, $W(\zeta)$, and $D(\zeta,\xi)$ are the gravity, gyroscopic, system actuator, lift and drag forces and moments, and external disturbances, respectively.

$$G = \begin{bmatrix} 0 & 0 & mg & 0 & 0 & 0 \end{bmatrix}^T$$
(19)

$$O(\zeta)\omega$$
 (20)

$$= \left[\sum_{i=1}^{4} \left(J_{prop} \left[\eta_{i} \Omega_{b} \times \begin{bmatrix} c_{\Theta_{i}} \\ 0 \\ -s_{\Theta_{i}} \end{bmatrix} \omega_{i} \right] \right) \right]$$

$$E(\xi) \omega^{2} = \begin{bmatrix} R_{b2i} F_{thru} \\ M_{thru} \end{bmatrix}$$
(21)
$$= \begin{bmatrix} (c_{\psi} c_{\theta} c_{\Theta_{tilt}} - (c_{\phi} s_{\theta} c_{\psi} + s_{\phi} s_{\psi}) s_{\Theta_{tilt}}) k U_{1} \\ (s_{\psi} c_{\theta} c_{\Theta_{tilt}} - (c_{\phi} s_{\theta} s_{\psi} - s_{\phi} c_{\psi}) s_{\Theta_{tilt}}) k U_{1} \\ (-s_{\theta} c_{\Theta_{tilt}} - c_{\phi} c_{\theta} s_{\Theta_{tilt}}) k U_{1} \\ s_{\Theta_{tilt}} k l_{s} U_{2} - c_{\Theta_{tilt}} k \lambda U_{3} \end{bmatrix}$$

$$\begin{bmatrix} s_{\Theta_{tilt}}kl_{l}U_{4} \\ c_{\Theta_{tilt}}kl_{s}U_{2} + s_{\Theta_{tilt}}k\lambda U_{3} \end{bmatrix}$$

where $U_{1} = (u_{1} + u_{2} + u_{3} + u_{4}), \quad U_{2} = (u_{1} + u_{2} + u_{3} + u_{4}), \quad U_{2} = (u_{1} + u_{2} + u_{3} + u_{4}), \quad U_{3} = (u_{1} + u_{2} + u_{3} + u_{4}), \quad U_{4} = (u_{1} + u_{2} + u_{3} + u_{4}), \quad U_{5} = (u_{1} + u_{2} + u_{3} + u_{4}), \quad U_{5} = (u_{1} + u_{2} + u_{3} + u_{4}), \quad U_{5} = (u_{1} + u_{2} + u_{3} + u_{4}), \quad U_{5} = (u_{1} + u_{2} + u_{3} + u_{4}), \quad U_{5} = (u_{1} + u_{3} + u_{4}), \quad U_{5} = (u_{1} + u_{5} + u_{5} + u_{5})$

 $(u_1 - u_2 + u_3 - u_4), \quad U_3 = (u_1 - u_2 - u_3 + u_4) \text{ and } U_4 = (u_1 + u_2 - u_3 - u_4).$

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$$W(\zeta) = \begin{bmatrix} F_{aero_x} \\ F_{aero_y} \\ F_{aero_z} \\ M_{aero_x} \\ M_{aero_y} \\ M_{aero_z} \end{bmatrix}$$
(22)
$$= \begin{bmatrix} R_{b2i} \begin{bmatrix} F_{D_1} + F_{D_2} + F_{D_3} + F_{D_4} \\ 0 \\ F_{L_1} + F_{L_2} + F_{L_3} + F_{L_4} \\ 0 \\ l_l (F_{L_1} + F_{L_2} - F_{L_3} - F_{L_4}) \\ 0 \end{bmatrix}$$

To simplify, all tilt angles are assumed to be equal to $(\Theta_1 = \Theta_2 = \Theta_3 = \Theta_4 = \Theta_{tilt})$. Control commands $u_{1,2,3,4}$ used in (21) are clearly written as:

$$\begin{bmatrix} u_1 & u_2 & u_3 & u_4 \end{bmatrix}^T = \begin{bmatrix} \omega_1^2 \\ \omega_2^2 \\ \omega_3^2 \\ \omega_4^2 \end{bmatrix}$$
(23)

Finally, the full dynamical model of the vehicle can be expressed as follows:

$$\dot{p} = f_1 + g_1 U_2 - g_1' U_3 \tag{24a}$$

$$\dot{q} = f_2 + g_2 U_4 \tag{24b}$$

$$\dot{r} = f_3 + g_3 U_2 + g_3' U_3$$
 (24c)

$$\dot{\phi} = p + q(s_{\phi}t_{\theta}) + r(c_{\phi}t_{\theta})$$
(24d)
$$\dot{\phi} = q q(s_{\phi}t_{\theta}) + r(c_{\phi}t_{\theta})$$
(24d)

$$\hat{\theta} = qc_{\phi} - rs_{\phi} \tag{24e}$$

$$\dot{\psi} = q \left(s_{\phi} \frac{1}{c_{\theta}} \right) + r \left(c_{\phi} \frac{1}{c_{\theta}} \right)$$

$$(24i)$$

$$X = f_4 + g_4 U_1 \tag{24g}$$

$$Y = f_5 + g_5 U_1$$
 (24n)
 $\ddot{Z} = f_6 + g_6 U_1$ (24i)

$$f_{1} = \frac{1}{I_{xx}} \left[(I_{yy} - I_{zz}) qr - J_{prop} qs_{\Theta_{tilt}} \omega_{p} \right]$$
(24a)

$$g_1 = \frac{k}{I_{xx}} [l_s s_{\Theta_{tilt}}] \tag{24b}$$

$$g_1' = \frac{k}{I_{xx}} \left[\lambda c_{\Theta_{tilt}} \right] \tag{24c}$$

$$f_{2} = \frac{1}{I_{yy}} \Big[(I_{zz} - I_{xx}) pr + J_{prop} \Big(ps_{\Theta_{tilt}} \Big) \Big]$$
(24d)

$$+ rc_{\Theta_{tilt}})\omega_p \\ + M_{aero_y} \Big]$$

$$g_2 = \frac{k}{I_{\gamma\gamma}} \left[l_l s_{\Theta_{tilt}} \right] \tag{24e}$$

$$f_3 = \frac{1}{I_{zz}} [(I_{xx} - I_{yy})pq$$
(24f)

$$-J_{prop}qc_{\Theta_{tilt}}\omega_p\right]$$

$$z_{tilt} = \frac{k}{2} \left[l_{tilt} = 1 \right]$$
(24g)

$$\begin{array}{c} y_3 - \frac{I_{zz}}{I_{zz}} [l_s c_{\Theta_{tilt}}] \\ k \end{array} \tag{24h}$$

$$g'_{3} = \frac{1}{I_{zz}} [\lambda s_{\Theta_{tilt}}]$$
(24i)

$$J_4 = -\frac{k}{m} r_{aero_X}$$
(24j)

$$g_{4} = m \frac{[c_{\psi}c_{\theta}c_{\theta}c_{\theta}_{tilt}]}{-(c_{\phi}s_{\theta}c_{\psi})} + s_{\phi}s_{\psi}s_{\theta_{tilt}}]$$

$$f_5 = \frac{1}{m} F_{aero_y} \tag{24k}$$

$$g_5 = \frac{k}{m} \left[s_{\psi} c_{\theta} c_{\Theta_{tilt}} \right]$$
(241)

$$- (c_{\phi} s_{\theta} s_{\psi}) - s_{\phi} c_{\psi} s_{\Theta_{tilt}}]$$

$$f_6 = \frac{1}{m} [mg + F_{aero_z}]$$
(24m)
$$k_z$$
(24m)

$$g_6 = \frac{\kappa}{m} \left[-s_\theta c_{\Theta_{tilt}} - c_\phi c_\theta s_{\Theta_{tilt}} \right]$$
(24n)

Where t_0 is tan () and $\omega_p = \omega_1 - \omega_2 - \omega_3 + \omega_4$.

Table 1: N	Jominal mod	deling parai	neters [25].

Symbol	Description	Magnitude
m_0	Mass	4.5 <i>kg</i>
l_{s_0}	Rotor distance to cog	0.3 m
0	along y axis	
l_{l_0}	Rotor distance to cog	0.3 m
0	along y axis	
I_{xx_0}	Moment of inertia	$0.405 \ kg \ m^2$
Ū	along x axis	
I_{yy_0}	Moment of inertia	$0.405 \ kg \ m^2$
	along y axis	
I_{zz_0}	Moment of inertia	0.72 kg m ²
0	along z axis	
λ_0	Torque/force ratio	0.01 Nm/N
k_0	Motor thrust constant	4.8×10^{-5}

Controller Design

The control design problem is to choose a control vector $[u_1 \ u_2 \ u_3 \ u_4]^T = [\omega_1^2 \ \omega_2^2 \ \omega_3^2 \ \omega_4^2]^T$ that compels the position

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and the attitude to track some desired commanded values in order to stabilize and accomplish a mission in the presence of parametric uncertainty. The tracking control problem can be achieved by keeping the system trajectory on the sliding surface S(t) = 0 [43]. The integral type sliding surface *S* is selected as

$$S(t) = \left(\frac{d}{dt} + \lambda_c\right)^n \left(\int_0^t e \, dt\right)$$
(26)

, where λ_c is a strictly positive constant that defines the bandwidth of the error dynamics and $n\$ is the order of differential equation. The sliding surface S(t) = 0 represents a linear differential equation whose solution implies

$$\int e(t)$$

The integral of tracking errors are used to cancel the steady-state errors [43]. In this paper, the development and the stability analysis of the controller do not use any linearization.

In order to control and to stabilize the attitude and altitude, with respect to (24), the states that must be controlled to track desired values Z_d , p_d , q_d and r_d are $[Z \ p \ q \ r]^T$. So, the sliding surfaces are defined by

$$S_{1} = \dot{e}_{z}(t) + 2\lambda_{c_{1}}e_{z}(t) + \lambda_{c_{1}}^{2}\int e_{z}(t)dt$$

$$S_{2} = e_{p}(t) + \lambda_{c_{2}}\int e_{p}(t)dt$$

$$S_{3} = e_{q}(t) + \lambda_{c_{3}}\int e_{q}(t)dt$$

$$S_{4} = e_{r}(t) + \lambda_{c_{4}}\int e_{r}(t)dt$$
Where
$$(27)$$

$$e_{z} = Z - Z_{d}$$

$$e_{p} = p - p_{d}$$

$$e_{q} = q - q_{d}$$

$$e_{r} = r - r_{d}$$
(28)

It is worth noting that, the desired angular velocities (p_d, q_d, r_d) are generated in controller by using the time derivative of the attitude angles and the velocity transformation matrix [25] and are defined as

$$\mathbb{E} = \begin{bmatrix} 1 & 0 & -s_{\theta} \\ 0 & c_{\phi} & s_{\phi}c_{\theta} \\ 0 & -s_{\phi} & c_{\phi}c_{\theta} \end{bmatrix}$$
(29)

$$\begin{bmatrix} p_d & q_d & r_d \end{bmatrix}^T = \mathbb{E} \cdot \begin{bmatrix} \dot{\phi}_d \\ \dot{\theta}_d \\ \dot{\psi}_d \end{bmatrix}$$
(30)

From equation (27) the derivatives of S are determined as

$$\dot{S}_1 = \ddot{e}_z(t) + 2\lambda_{c_1}\dot{e}_z(t) + \lambda_{c_1}^2 e_z(t)$$
⁽³¹⁾

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 $\dot{S}_4 = \dot{e}_r(t) + \lambda_{c_4} e_r(t)$

By using (28), (24), and (25) and substituting them into (31), the equations become

$$\dot{S}_{1} = -\ddot{Z}_{d} + f_{6} + 2\lambda_{c_{1}}\dot{e}_{z}(t) + \lambda_{c_{1}}^{2}e_{z}(t) + g_{6}U_{1}$$
(32a)

$$\dot{S}_2 = -\dot{p}_d + f_1 + \lambda_{c_2} e_p(t) + g_1 U_2$$
 (32b)
 $-g'_1 U_3$

$$\dot{S}_3 = -\dot{q}_d + f_2 + \lambda_{c_3} e_q(t) + g_2 U_4$$
 (32c)

$$\dot{S}_4 = -\dot{r}_d + f_3 + \lambda_{c_4} e_r(t) + g_3 U_2 \qquad (32d) + g'_3 U_3$$

, which can be written as a vector form

гċл

$$\begin{bmatrix} S_{1} \\ \dot{S}_{2} \\ \dot{S}_{3} \\ \dot{S}_{4} \end{bmatrix} = \begin{bmatrix} v_{1} \\ v_{2} \\ v_{3} \\ v_{4} \end{bmatrix} +$$

$$\begin{bmatrix} g_{6} & g_{6} & g_{6} & g_{6} \\ g_{1} - g_{1}' & -g_{1} + g_{1}' & g_{1} + g_{1}' & -g_{1} - g_{1}' \\ g_{2} & g_{2} & -g_{2} & -g_{2} \\ g_{3} + g_{3}' & g_{3} + g_{3}' & g_{3} + g_{3}' & g_{3} + g_{3}' \end{bmatrix} \begin{bmatrix} u_{1} \\ u_{2} \\ u_{3} \\ u_{4} \end{bmatrix}$$

$$Where$$

$$v_{1} = -\ddot{Z}_{d} + f_{6} + 2\lambda_{c_{1}}\dot{e}_{z}(t) + \lambda_{c_{1}}^{2}e_{z}(t)$$

$$v_{2} = -\dot{p}_{d} + f_{1} + \lambda_{c_{2}}e_{p}(t)$$

$$v_{3} = -\dot{q}_{d} + f_{2} + \lambda_{c_{3}}e_{q}(t)$$

$$v_{4} = -\dot{r}_{d} + f_{3} + \lambda_{c_{4}}e_{r}(t)$$

$$(33)$$

To simplify, the equation (33) can be rewritten as a compact form:

$$\dot{S} = v + Gu \tag{35}$$

The purpose of keeping the scalar \$S\$ at zero, it can now be achieved by choosing the control commands $[u_1 \ u_2 \ u_3 \ u_4]^T$ to satisfy the sliding condition equations [43]

$$\frac{1}{2}\frac{dS_i^2}{dt} \le -\sigma_i |S_i|; \quad i = 1, 2, 3, 4$$
(35)

, where σ_i (i = 1,2,3,4), are strictly positive constants that can be chosen in order to set the desired reaching time to the sliding surfaces [44]. The equation (36) indicates that the squared distance to the surface, as measured by S^2 decreases along all system trajectories [43]. With respect to (36), it is tuned that

$$\sigma_{1} = sgn(S_{1})\dot{S}_{1} + 0.900$$

$$\sigma_{2} = sgn(S_{2})\dot{S}_{2} + 0.037$$

$$\sigma_{3} = sgn(S_{3})\dot{S}_{3} + 0.040$$

$$\sigma_{4} = sgn(S_{4})\dot{S}_{4} + 0.008$$
(37)

By using (35), the controller which satisfies the sliding conditions (36) can be define as

$$u = G^{-1}[-v - \sigma \, sgn(S)] \tag{38}$$

, where *G* is assumed to be invertible. This control law can be considered as two parts as equivalent control that be shown as $G^{-1}[-v]$, which guarantees $\dot{S} = 0$, for the nominal model, and the other term defined as $G^{-1}[-\sigma sgn(S)]$, handles parameter uncertainties and disturbances. It is important to stress that in the presence of modeling imprecision, the control law becomes discontinuous and this leads to chattering.

The chattering is undesirable since it involves high control action and may excite high-frequency dynamics that are neglected in the modeling. Thus, it must be eliminated by smoothing out the controller discontinuity in a thin boundary layer neighboring the switching surface [43]. This can be achieved by defining the thin boundary layers of widths Φ around the sliding surfaces. Therefore, replacing sgn(S) with continuous saturation functions $sat(\frac{s}{\Phi})$. So, the equation (38) can be rewritten as:

$$u = G^{-1} \left[-\nu - \sigma \operatorname{sat}(\frac{s}{\Phi}) \right]$$
(39)

The parameter uncertainties are modeled by an additive variance Δ to the nominal values, used for controlling development. To illustrate this modeling imprecision, only a limited number of uncertainties are considered [45].

$$m = m_0 (1 + \Delta m) \tag{40a}$$

$$I_{xx} = I_{xx_0} (1 + \Delta I_{xx})$$
(40b)

$$I_{yy} = I_{yy_0} (1 + \Delta I_{yy})$$
 (40c)

$$I_{zz} = I_{zz_0} (1 + \Delta I_{zz})$$
(40d)

, where the nominal values are illustrated in Table 1, and the additive uncertainties values are taken as follow

$$|\Delta m| \le 0.1 \tag{41a}$$

$$|\Delta I_{xx}| \le 0.2 \tag{41b}$$

$$\Delta I_{yy} \Big| \le 0.2 \tag{41c}$$

$$|\Delta I_{zz}| \le 0.2 \tag{41d}$$

Finally, the control law considering the parameter uncertainties can be defined as

$$\begin{bmatrix} u_1\\u_2\\u_3\\u_4 \end{bmatrix}$$

$$= (G + G\Delta G)^{-1} \begin{bmatrix} -(v_1 + f_6\Delta f_6) - \sigma_1 sat(\frac{S_1}{\Phi_1}) \\ -(v_2 + f_1\Delta f_1) - \sigma_2 sat(\frac{S_2}{\Phi_2}) \\ -(v_3 + f_2\Delta f_2) - \sigma_3 sat(\frac{S_3}{\Phi_3}) \\ -(v_4 + f_3\Delta f_3) - \sigma_4 sat(\frac{S_4}{\Phi_4}) \end{bmatrix}$$
(42)

so, the compact form is

$$u = \hat{G}^{-1} \left[-\hat{v} - \sigma \operatorname{sat}(\frac{s}{\Phi}) \right]$$
(43)

that ΔG and Δf_i (i = 6, 1, 2, 3), are created due to uncertainties (40), which are applied on f and g (25), in control design. Also, \hat{G} and \hat{v} , are chosen estimated of G and v, respectively.

For verification of the proposed nonlinear controller, a linear based controller is designed and considered for comparison. For developing the linear based controller, it is assumed that in the set of equations (24)

$$\phi \approx 0 \tag{44a}$$

$$\theta \approx 0$$
 (44b)

$$\psi \approx 0 \tag{44c}$$

$$\dot{p} \approx \phi$$
 (44d)

$$\dot{q} \approx \theta$$
 (44e)
 $\dot{r} \approx \ddot{\psi}$ (44f)

then, the control law is redesigned and simulation results are compared with the proposed controller.

Simulation Results

The performance of the sliding mode controller is evaluated on the nonlinear dynamic model of the tilt-wing UAV in MATLAB/Simulink. It should be recalled that the desired commands in these simulations are filtered by a low-pass filter because they are subjected to derivation in the process of controller development and it is achieved by smoothing the command signals.

Also, the sliding boundary layers Φ_i are tuned as 0.01 for all surfaces. Starting with all zero initial configurations of the UAV. Additionally, the tilt angles for all wings are selected as $\Theta_{tilt} = \frac{\pi}{2}$ during the flight mission. With this assumption, aerodynamics moments are equal to zero.

The sliding mode control conducted really well in tracking the reference command inputs. Figure 4 and Figure 5 illustrate the response of sliding mode controller to track the desired altitude and attitude

commands signal, respectively. These figures show that the proposed controller handled the tracking of command signals in appropriate time length in the presence of uncertainties. Note that, Figure 6 and Figure 7 show the control errors and the control efforts of the controller defined as square of rotors rotation, respectively. From the tracking error figure it can be inferred that the controller response is acceptable.

It is significant to emphasize that the control effort is small enough and the magnitude of the motor forces that need to be generated do not overcome the physical limits ($\simeq 16$ N) of the rotors [21] (see Figure 8). To illustrate that the sliding surfaces tend to zero, its values are shown during the simulation in Figure 9.

In this paper, there are no control efforts on X and Y direction of the vehicle. Figure 10 shows the 3D trajectory of UAV's center of mass. In Figure 11 time-history of accelerations are shown. Results illustrate that linear and angular accelerations are in an acceptable range. The Figure 12 is given to show the values of linear and angular velocities during the simulation. Also, the need to use a controller based on a nonlinear system is illustrated in Figures 13 and 14 with comparison of sensitivity of controllers in the presence of pitch noise (Figure 15) and pitch moment disturbance (Figure 16).

Conclusion and Future Works

In this paper, a MIMO integral type sliding mode controller is developed in several stages for the nonlinear model of the tilt-wing UAV that can take-off and land vertically. This controller is able to deal with parameter uncertainties due to modeling imprecision. It is necessary to mention that in development of the controller, there is no linearization. Simulations conducted show that the controller has good tracking performance and robustness in the presence of uncertainties.

We have indicated our work on controller design on a new tilt-wing aerial vehicle. Future works will incorporate advances and improvements on the controller in combination with adaptation. Additionally, the effects of tilt angle of wing and the uncertainty it produces will be analyzed. Sliding mode stabilization of quad tilt-wing UAV Considering Nonlinear Model of the Vehicle and Uncertainties

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Controller.



Figure 7: Control Effort in Sliding Mode Controller.







Figure 10: 3D Trajectory of the Vehicle Center of Mass.







Figure 13: Pitch Control Using Sliding Mode Controller Based on Linear Dynamics in the Presence of Noise and Disturbance.



Figure 14: Pitch Control Using Sliding Mode Controller Based on nonlinear Dynamics in the Presence of Noise and Disturbance.



Sliding mode stabilization of quad tilt-wing UAV Considering Nonlinear Model of the Vehicle and Uncertainties



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